

Program: SE Information Technology

Curriculum Scheme: Rev-2019

Examination: Second year semester III

Course Code: ITC301 and Course Name: Engineering Mathematics-III

MCQ_SECTION

Time: 40 Min

Max. Marks: 40

1] All questions are Compulsory

2] Assume suitable data wherever required.

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| Q1. | $L[t^{\frac{5}{2}}]$ is |
| Option A: | $\frac{3}{4s^{\frac{3}{2}}}$ |
| Option B: | $\frac{3\sqrt{\pi}}{4s^{\frac{5}{2}}}$ |
| Option C: | $\frac{5\sqrt{\pi}}{4s^{\frac{5}{2}}}$ |
| Option D: | $\frac{15\sqrt{\pi}}{8s^{\frac{7}{2}}}$ |
| | |
| Q2. | $L [f(t)] = \frac{1}{s\sqrt{s+1}}$ then $L [e^{-2t}f(t)]$ is |
| Option A: | $\frac{1}{(s+2)\sqrt{s+3}}$ |
| Option B: | $\frac{1}{(s+2)\sqrt{s+2}}$ |
| Option C: | $\frac{1}{(s-2)\sqrt{s-1}}$ |

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| Option D: | $\frac{1}{(s-1)\sqrt{s}}$ |
| Q3. | Find $L^{-1} \left[\frac{s+2}{(s+2)^2-16} \right]$ |
| Option A: | $e^{2t} \cosh 4t$ |
| Option B: | $e^{-2t} \sinh 4t$ |
| Option C: | $e^{-2t} \cosh 4t$ |
| Option D: | $e^{2t} \sinh 4t$ |
| Q4. | Find $L^{-1} \left[\frac{1}{(s+4)^{3/2}} \right]$ |
| Option A: | $2e^{4t} \sqrt{\frac{\pi}{t}}$ |
| Option B: | $e^{-4t} \sqrt{\frac{\pi}{t}}$ |
| Option C: | $e^{4t} \sqrt{\frac{t}{\pi}}$ |
| Option D: | $2e^{-4t} \sqrt{\frac{t}{\pi}}$ |
| Q5. | The probability that a 3-card hand drawn at random and without replacement from an ordinary deck consist entirely of black card is: |
| Option A: | $\frac{1}{17}$ |
| Option B: | $\frac{3}{17}$ |
| Option C: | $\frac{2}{17}$ |
| Option D: | $\frac{1}{8}$ |
| Q6. | A, B, C hit a target with probabilities $1/2$, $2/3$, $3/4$ respectively. If all of them fire at the target, the probability p that at least one of them hits the target is: |

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| Option A: | $\frac{1}{24}$ |
| Option B: | $\frac{23}{24}$ |
| Option C: | $\frac{7}{12}$ |
| Option D: | $\frac{11}{12}$ |
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| Q7. | The probability density function of a discrete random variable X is given by the formula $P(x) = kx^2, x = 0,1,2,3$; the value of constant k is: |
| Option A: | $\frac{1}{14}$ |
| Option B: | $\frac{3}{2}$ |
| Option C: | $\frac{1}{6}$ |
| Option D: | 6 |
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| Q8. | The expected value for a random variable is |
| Option A: | the long-run average. |
| Option B: | the most likely value. |
| Option C: | the most frequent value observed in a random sample of observations of the random variable. |
| Option D: | always np. |
| | |
| Q9. | The function $f(z) = e^z$ is |
| Option A: | Analytic |
| Option B: | Hyperbolic |
| Option C: | Not Analytic |
| Option D: | Elliptic |
| | |
| Q10. | The imaginary part of $f(z) = \cos z$ is |
| Option A: | $-\sin x \cosh y$ |
| Option B: | $\cosh x \cos y$ |
| Option C: | $-\sin x \sinh y$ |
| Option D: | $\sin x \sinh y$ |

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| Q11. | The analytic function corresponding to real part $e^{-x} \sin y$ is |
| Option A: | $f(z) = e^z + c$ |
| Option B: | $f(z) = e^{-z} + c$ |
| Option C: | $f(z) = ie^z + c$ |
| Option D: | $f(z) = ie^{-z} + c$ |
| Q12. | The analytic function corresponding to imaginary part $3x^2y - y^3$ is |
| Option A: | $f(z) = z^2 + c$ |
| Option B: | $f(z) = z^3 + c$ |
| Option C: | $f(z) = -z^2 + c$ |
| Option D: | $f(z) = -z^3 + c$ |
| Q13. | Which of these is not Dirichlet's conditions for a function $f(x)$ to be expanded in a Fourier series in the interval $(0, 2L)$ |
| Option A: | $f(x)$ may have discontinuities, finite in number |
| Option B: | $f(x)$ may have maxima and minima, finite in number |
| Option C: | $f(x)$ is single valued |
| Option D: | $f(x)$ is always an even function |
| Q14. | If $f(x)$ is an odd function, then the Fourier series for $f(x)$ is a |
| Option A: | Cosine series |
| Option B: | Sine series |
| Option C: | Contains both sine series and cosine series |
| Option D: | neither sine series nor cosine series |
| Q15. | The fourier series for $f(x) = \sin x $ in $[-\pi, \pi]$ |
| Option A: | Will have sine terms |
| Option B: | Will have cosine terms |
| Option C: | Is zero |
| Option D: | Doesn't exist |
| Q16. | If $f(x) = x^2$ in $[-\pi, \pi]$ then what is the value of the first term in the series $\frac{a_0}{2} + \sum_{n=1}^{\infty} a_n \cos nx + \sum_{n=1}^{\infty} b_n \sin nx$ |
| Option A: | $\frac{\pi^2}{3}$ |
| Option B: | $\frac{\pi^2}{6}$ |

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| Option C: | $\frac{\pi^2}{2}$ |
| Option D: | $\frac{\pi}{3}$ |
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| Q17. | The slope of the line of regression of y on x is called_____ |
| Option A: | Coefficient of correlation |
| Option B: | Rank correlation coefficient |
| Option C: | Regression coefficient of y on x |
| Option D: | Regression coefficient of x on y |
| | |
| Q18. | Correlation coefficient is the _____ mean between the regression coefficients |
| Option A: | Arithmetic |
| Option B: | Geometric |
| Option C: | Harmonic |
| Option D: | Weighted |
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| Q19. | Regression coefficient are independent of the |
| Option A: | Change of origin |
| Option B: | Change of scale |
| Option C: | Change of origin but not scale |
| Option D: | Change of origin and scale |
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| Q20. | Let the regression equation of y on x be $x - 2y + 5 = 0$ then b_{yx} is equal to |
| Option A: | -2 |
| Option B: | 1 |
| Option C: | 5 |
| Option D: | $\frac{1}{2}$ |

DESCRIPTIVE_SECTION

Time: 1.20 Hrs.

Max. Marks: 40

Attempt all questions.

| Q2 | Solve any Four out of six | 5 Marks each |
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| A | Find Laplace Transformation of $t\sqrt{1 + \sin t}$ | |
| B | Find $L^{-1}\left(\frac{(s+3)}{(s^2+6s+13)^2}\right)$ using Convolution Theorem | |
| C | If $f(x) = 9 - x^2$ for $-3 < x < 3$, obtain Fourier series of $f(x)$ in $[-3, 3]$. | |
| D | Construct the analytic function whose real part is $e^{2x}(x \cos 2y - y \sin 2y)$ | |
| E | The no. of pairs of observation of x and y are 1000. $\sigma_x = 4.5$; $\sigma_y = 3.6$; $\sum (x - \bar{x})(y - \bar{y}) = 4800$ Calculate the coefficient of correlation between x and y series. | |
| F | In a certain college, 4% of the boys and 1% of the girls are taller than 1.8m. Furthermore 60% of the students are girls. If the students are selected at random and found to be taller than 1.8m, what is the probability that the student is a girl? | |
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| Q3 | Solve any Four out of six | 5 Marks each |
| A | Find Laplace transformation of $\frac{e^{-2t} \sin(2t) \cosh t}{t}$ | |
| B | Find the half range sine series of $f(x) = x^2$ in $(0, \pi)$ | |
| C | Find the orthogonal trajectories of the family of curves $3x^2y - y^3 = c$ | |
| D | The two regression lines are $4x - 5y + 33 = 0$; $20x - 9y = 107$ and variance of $x = 25$. Find i) mean of x & y ii) Coefficient of correlation | |

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| | iii) Variance of y |
| E | Two persons A and B toss an unbiased coin alternately on the understanding that the first who gets head wins. If A starts the game, find their respective chance of winning. |
| F | Find $L^{-1} \left(\frac{2s^2 - 15s - 11}{(s + 2)(s - 3)^2} \right)$ |