

Sample Question Paper

Examination: S.E.

Branch: Information Technology

Semester -IV(Rev2012)

Course Name: Applied Mathematics – IV(CBGS)

Time: 1 hour

All the Questions are compulsory and carry equal marks .

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| Q1. | If the eigen values of A are 1,2,3 then the matrix is |
| Option A: | derogatory |
| Option B: | Non derogatory |
| Option C: | Identity matrix |
| Option D: | Singular |
| Q2. | If the geometric multiplicity is same as the algebraic multiplicity of each eigen value of the then the matrix A then A is |
| Option A: | Non diagonalizable |
| Option B: | Diagonalizable |
| Option C: | Null matrix |
| Option D: | Hermitian matrix |
| Q3. | The value of the integral $\int_c \frac{\cos z}{(z+\pi)^3} dz$ where $c: z = 2$ is |
| Option A: | 1 |
| Option B: | $2\pi i$ |
| Option C: | -1 |
| Option D: | 0 |
| Q4. | If $f(z) = \frac{2z+1}{(z+1)(z+2)^2}$ then the order of the pole $Z = -1$ and $Z = -2$ respectively |
| Option A: | 1 and 2 |
| Option B: | -1 and -2 |
| Option C: | 0 and 0 |
| Option D: | 2 and 1 |
| Q5. | The optimum solution of the LPP $\text{Max } Z = x_1 + 4x_2$ subject to the constraints $2x_1 + x_2 \leq 3$ $3x_1 + 5x_2 \leq 9$ and $x_1, x_2 \geq 0$ |
| Option A: | $(0, \frac{9}{5})$ |
| Option B: | (0,0) |
| Option C: | $(\frac{6}{7}, \frac{9}{7})$ |
| Option D: | $(\frac{3}{2}, 0)$ |
| Q6. | If $f(z) = z^3 + z^2 + \frac{z}{2!} + \frac{1}{3!} + \frac{1}{4!z} + \frac{1}{5!z^2} + \dots$ then residue at $z = 0$ is |

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| Option A: | $\frac{1}{4!}$ |
| Option B: | 2! |
| Option C: | 4! |
| Option D: | 5! |
| | |
| Q7. | If the objective function is of the minimization type then the coefficient of the artificial variable in the big M method is |
| Option A: | 0 |
| Option B: | 1 |
| Option C: | M |
| Option D: | -M |
| | |
| Q8. | The dual of the Primal Max $Z=7x_1 + 2x_2$ subject to $4x_1 + 5x_2 \leq 2$ $3x_1 - x_2 \leq 9$ where $x_1, x_2 \geq 0$ is |
| Option A: | Max $W = 2w_1 + 9w_2$ subject to $4w_1 + 3w_2 \geq 7$ $5w_1 - w_2 \geq 2$ where $w_1, w_2 \geq 0$ |
| Option B: | Min $W = 2w_1 + 9w_2$ subject to $4w_1 + 3w_2 \geq 7$ $5w_1 - w_2 \geq 2$ where $w_1, w_2 \geq 0$ |
| Option C: | Min $W = 2w_1 + 9w_2$ subject to $4w_1 + 3w_2 \leq 7$ $5w_1 - w_2 \leq 2$ where $w_1, w_2 \geq 0$ |
| Option D: | Min $W = 2w_1 + 9w_2$ subject to $4w_1 + 3w_2 = 7$ $5w_1 - w_2 = 2$ where $w_1, w_2 \geq 0$ |
| | |
| Q9. | If $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ then A^{-1} is |
| Option A: | $\begin{bmatrix} 2 & 2 \\ 3 & 8 \end{bmatrix}$ |
| Option B: | $\begin{bmatrix} 1 & 2 \\ 0 & 4 \end{bmatrix}$ |
| Option C: | $\begin{bmatrix} 2 & 2 \\ 3 & 4 \end{bmatrix}$ |
| Option D: | $\begin{bmatrix} 2 & 4 \\ 6 & 8 \end{bmatrix}$ |
| | |
| Q10. | The dual of the dual is |
| Option A: | Dual |
| Option B: | Doesn't exist |
| Option C: | Primal |
| Option D: | In the canonical form |
| | |
| Q11. | The $\int_c (z + z^2) dz$ where $ z =2$ |
| Option A: | $4\pi i$ |
| Option B: | 4π |
| Option C: | $4i$ |

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| Option D: | 0 |
| Q12. | For the function $f(z) = \frac{1-\cos z}{z^3}$, $z=0$ is |
| Option A: | Pole of order 1 |
| Option B: | Essential singularity |
| Option C: | Removable singularity |
| Option D: | Zero of $f(z)$ |
| Q13. | Value of the integral $\int_c \frac{\sin z}{z - \frac{\pi}{2}} dz =$ |
| Option A: | $-2\pi i$ |
| Option B: | $2\pi i$ |
| Option C: | $-\pi i$ |
| Option D: | πi |
| Q14. | In a standard form of a LPP the constraints are of the type |
| Option A: | \geq |
| Option B: | \leq |
| Option C: | $=$ |
| Option D: | $<$ |
| Q15. | The statement “ If $f(z)$ is analytic in a region bounded by a simple closed curve c except at the point $z=a$, then $\int_c \frac{f(z)}{z-a} dz = 2\pi i f(a)$ ” is |
| Option A: | Cauchy’s theorem |
| Option B: | Cauchy’s Integral theorem |
| Option C: | Residue theorem |
| Option D: | Taylor’s Theorem |
| Q16. | A continuous random variable has probability density function $f(x) = x - x^2; 0 \leq x \leq 1$. Find Mean |
| Option A: | $\frac{1}{12}$ |
| Option B: | $\frac{1}{3}$ |
| Option C: | $\frac{1}{6}$ |
| Option D: | $\frac{5}{3}$ |
| Q17. | A Binomial Distribution of a random variable X is $P(X = r) = {}^6C_r \left(\frac{1}{4}\right)^r \left(\frac{3}{4}\right)^{6-r}$ then find Variance of X |
| Option A: | $\frac{3}{4}$ |
| Option B: | $\frac{9}{8}$ |
| Option C: | $\frac{1}{4}$ |
| Option D: | $\frac{3}{8}$ |

| Q18. | The Probability density function of a random variable X is <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>X</th> <th>1</th> <th>2</th> <th>3</th> <th>4</th> <th>5</th> </tr> </thead> <tbody> <tr> <td>P(X=x)</td> <td>4k</td> <td>5k</td> <td>6k</td> <td>9k</td> <td>10k</td> </tr> </tbody> </table> <p>Find $P(1 < X \leq 4)$</p> | X | 1 | 2 | 3 | 4 | 5 | P(X=x) | 4k | 5k | 6k | 9k | 10k |
|-----------|---|----|----|----|-----|---|---|--------|----|----|----|----|-----|
| X | 1 | 2 | 3 | 4 | 5 | | | | | | | | |
| P(X=x) | 4k | 5k | 6k | 9k | 10k | | | | | | | | |
| Option A: | $\frac{10}{17}$ | | | | | | | | | | | | |
| Option B: | $\frac{12}{17}$ | | | | | | | | | | | | |
| Option C: | $\frac{13}{17}$ | | | | | | | | | | | | |
| Option D: | $\frac{15}{17}$ | | | | | | | | | | | | |
| Q19. | If a random variable X follows Poisson distribution such that $P(X = 1) = 2P(X = 2)$ then find the value of $P(X = 4)$ | | | | | | | | | | | | |
| Option A: | 0.07754 | | | | | | | | | | | | |
| Option B: | 0.01532 | | | | | | | | | | | | |
| Option C: | 0.08945 | | | | | | | | | | | | |
| Option D: | 0.06879 | | | | | | | | | | | | |
| Q20. | The Moment Generating Function about origin of a random variable is $M_0(t) = \frac{3}{3-t}$. Find Mean | | | | | | | | | | | | |
| Option A: | $\frac{2}{3}$ | | | | | | | | | | | | |
| Option B: | $\frac{1}{3}$ | | | | | | | | | | | | |
| Option C: | $\frac{5}{3}$ | | | | | | | | | | | | |
| Option D: | $\frac{4}{3}$ | | | | | | | | | | | | |
| Q21. | If a sample point lies in the critical region then | | | | | | | | | | | | |
| Option A: | Null Hypothesis is Accepted and Alternate Hypothesis is Rejected | | | | | | | | | | | | |
| Option B: | Null Hypothesis is Rejected and Alternate Hypothesis is Accepted | | | | | | | | | | | | |
| Option C: | Both Null Hypothesis and Alternate Hypothesis are Accepted | | | | | | | | | | | | |
| Option D: | Both Null Hypothesis and Alternate Hypothesis are Rejected | | | | | | | | | | | | |
| Q22. | small sample test is used when | | | | | | | | | | | | |
| Option A: | sample size $n < 30$ | | | | | | | | | | | | |
| Option B: | sample size $n \geq 30$ | | | | | | | | | | | | |
| Option C: | sample size $n = 40$ | | | | | | | | | | | | |
| Option D: | sample size $n = 50$ | | | | | | | | | | | | |
| Q23. | If a random variable X follows Poisson distribution such that $P(X = 0) = 6P(X = 3)$ then find the value of $P(X = 4)$ | | | | | | | | | | | | |

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|-----------|---|----|----|----|----|-----|-----|-----|---|---|--------|---|----|----|----|----|-----|-----|-----|
| Option A: | 0.07754 | | | | | | | | | | | | | | | | | | |
| Option B: | 0.01532 | | | | | | | | | | | | | | | | | | |
| Option C: | 0.08945 | | | | | | | | | | | | | | | | | | |
| Option D: | 0.06879 | | | | | | | | | | | | | | | | | | |
| Q24. | A Binomial Distribution of a random variable X is $P(X = r) = {}^{10}C_r \left(\frac{1}{5}\right)^r \left(\frac{4}{5}\right)^{10-r}$ then find Variance of X | | | | | | | | | | | | | | | | | | |
| Option A: | $\frac{3}{5}$ | | | | | | | | | | | | | | | | | | |
| Option B: | $\frac{9}{10}$ | | | | | | | | | | | | | | | | | | |
| Option C: | $\frac{1}{5}$ | | | | | | | | | | | | | | | | | | |
| Option D: | $\frac{8}{5}$ | | | | | | | | | | | | | | | | | | |
| Q25. | The Probability density function of a random variable X is <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>X</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> </tr> <tr> <td>P(X=x)</td> <td>k</td> <td>3k</td> <td>5k</td> <td>7k</td> <td>9k</td> <td>11k</td> <td>13k</td> <td>15k</td> </tr> </table> Find $P(2 < X \leq 5)$ | X | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | P(X=x) | k | 3k | 5k | 7k | 9k | 11k | 13k | 15k |
| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | | | | | | | | | | | |
| P(X=x) | k | 3k | 5k | 7k | 9k | 11k | 13k | 15k | | | | | | | | | | | |
| Option A: | $\frac{5}{8}$ | | | | | | | | | | | | | | | | | | |
| Option B: | $\frac{27}{64}$ | | | | | | | | | | | | | | | | | | |
| Option C: | $\frac{1}{2}$ | | | | | | | | | | | | | | | | | | |
| Option D: | $\frac{55}{64}$ | | | | | | | | | | | | | | | | | | |