



**Mahavir Education Trust's**  
**SHAH & ANCHOR KUTCHHI ENGINEERING COLLEGE**  
Chembur, Mumbai - 400 088

**Subject:** Applied Mathematics – IV

**Branch:** Information Technology

**Sem – IV (CBCS)**

**Time:** 1 hour

**Max. Marks:** 50

**Sample Question Paper**

Instructions: 1] All the Questions are compulsory and carry equal marks

2]. All Questions are Multiple Choice Questions

3] Select the correct answer from the Choices

|           |   |
|-----------|---|
| Q1.       | A continuous random variable has probability density function $f(x) = x - x^2; 0 \leq x \leq 1$ . Find Mean                             |
| Option A: | $\frac{1}{12}$  |
| Option B: | $\frac{1}{3}$   |
| Option C: | $\frac{1}{6}$   |
| Option D: | $\frac{5}{3}$   |
|           |   |
| Q2.       | A connected planar graph has 10 vertices each of degree 3. In how many ways does a representation of this planar graph split the plane? |
| Option A: | 6   |
| Option B: | 5   |
| Option C: | 7   |
| Option D: | 8   |
|           |   |
| Q3.       | The simplest form of Boolean Expression $(A + B)(A + C)$ is   |
| Option A: | $A + BC$  |
| Option B: | $BC$  |
| Option C: | $ABC$   |
| Option D: | $A + B + C$   |
|           |   |
| Q4.       | Small sample test is used when  |

|           |   |
|-----------|---|
| Option A: | sample size $n < 30$  |
| Option B: | sample size $n \geq 30$   |
| Option C: | sample size $n = 40$  |
| Option D: | sample size $n = 50$  |
|           |   |
| Q5.       | By Euclidean Algorithm, the Greatest Common Divisor of 112 and 144 is _____   |
| Option A: | 6   |
| Option B: | 16  |
| Option C: | 4   |
| Option D: | 8   |
|           |   |
| Q6.       | Given that $G = \{x \mid x = a + \sqrt{2} b, a \text{ & } b \text{ are real numbers}\}$ is a group under usual multiplication. Find the multiplicative identity element of the group. |
| Option A: | a   |
| Option B: | b   |
| Option C: | ab  |
| Option D: | 1   |
|           |   |
| Q7.       | Given that $L = \{1, 3, 5, 9, 15, 45\}$ is a Bounded Lattice under the relation divisibility. Find the Greatest element of the Lattice $L$ .  |
| Option A: | 1   |
| Option B: | 45  |
| Option C: | 15  |
| Option D: | 3   |
|           |   |
| Q8.       | If $15x \equiv 6 \pmod{9}$ then $x =$ _____   |
| Option A: | 6   |
| Option B: | 8   |
| Option C: | 4   |
| Option D: | 3   |
|           |   |
| Q9.       | A Binomial Distribution of a random variable X is $P(X = r) = {}^6C_r \left(\frac{1}{4}\right)^r \left(\frac{3}{4}\right)^{6-r}$ then find Variance of X                              |
| Option A: | $\frac{3}{4}$   |
| Option B: | $\frac{9}{8}$   |
| Option C: | $\frac{1}{4}$   |
| Option D: | $\frac{3}{8}$   |
|           |   |

|           |   |    |    |    |     |   |   |        |    |    |    |    |     |
|-----------|---|----|----|----|-----|---|---|--------|----|----|----|----|-----|
| Q10.      | If $2x + 3y + 8 = 0$ and $x + 2y - 5 = 0$ are regression lines then means of $x$ & $y$ are  |    |    |    |     |   |   |        |    |    |    |    |     |
| Option A: | $\bar{x} = -11$ & $\bar{y} = 8$   |    |    |    |     |   |   |        |    |    |    |    |     |
| Option B: | $\bar{x} = 25$ & $\bar{y} = 13$   |    |    |    |     |   |   |        |    |    |    |    |     |
| Option C: | $\bar{x} = -5$ & $\bar{y} = 7$  |    |    |    |     |   |   |        |    |    |    |    |     |
| Option D: | $\bar{x} = -31$ & $\bar{y} = 18$  |    |    |    |     |   |   |        |    |    |    |    |     |
|           |   |    |    |    |     |   |   |        |    |    |    |    |     |
| Q11.      | A connected planar graph has 9 vertices having degrees 2, 2, 2, 3, 3, 3, 4, 4 and 5. How many edges are there in the graph?   |    |    |    |     |   |   |        |    |    |    |    |     |
| Option A: | 12  |    |    |    |     |   |   |        |    |    |    |    |     |
| Option B: | 13  |    |    |    |     |   |   |        |    |    |    |    |     |
| Option C: | 14  |    |    |    |     |   |   |        |    |    |    |    |     |
| Option D: | 15  |    |    |    |     |   |   |        |    |    |    |    |     |
|           |   |    |    |    |     |   |   |        |    |    |    |    |     |
| Q12.      | Find value of Jacobi's symbol $\left(\frac{102}{37}\right)$   |    |    |    |     |   |   |        |    |    |    |    |     |
| Option A: | -1  |    |    |    |     |   |   |        |    |    |    |    |     |
| Option B: | 0   |    |    |    |     |   |   |        |    |    |    |    |     |
| Option C: | -2  |    |    |    |     |   |   |        |    |    |    |    |     |
| Option D: | 1   |    |    |    |     |   |   |        |    |    |    |    |     |
|           |   |    |    |    |     |   |   |        |    |    |    |    |     |
| Q13.      | Integral solution of the equation $55x + 34y = 36$ is   |    |    |    |     |   |   |        |    |    |    |    |     |
| Option A: | $x = 16$ & $y = -21$  |    |    |    |     |   |   |        |    |    |    |    |     |
| Option B: | $x = 15$ & $y = 23$   |    |    |    |     |   |   |        |    |    |    |    |     |
| Option C: | $x = 26$ & $y = -41$  |    |    |    |     |   |   |        |    |    |    |    |     |
| Option D: | $x = 20$ & $y = -11$  |    |    |    |     |   |   |        |    |    |    |    |     |
|           |   |    |    |    |     |   |   |        |    |    |    |    |     |
| Q14.      | The Probability density function of a random variable X is  |    |    |    |     |   |   |        |    |    |    |    |     |
|           | <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>X</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr> <tr> <td>P(X=x)</td><td>4k</td><td>5k</td><td>6k</td><td>9k</td><td>10k</td></tr> </table> | X  | 1  | 2  | 3   | 4 | 5 | P(X=x) | 4k | 5k | 6k | 9k | 10k |
| X         | 1   | 2  | 3  | 4  | 5   |   |   |        |    |    |    |    |     |
| P(X=x)    | 4k  | 5k | 6k | 9k | 10k |   |   |        |    |    |    |    |     |
|           | Find $P(1 < X \leq 4)$  |    |    |    |     |   |   |        |    |    |    |    |     |
| Option A: | $\frac{10}{17}$   |    |    |    |     |   |   |        |    |    |    |    |     |
| Option B: | $\frac{12}{17}$   |    |    |    |     |   |   |        |    |    |    |    |     |
| Option C: | $\frac{13}{17}$   |    |    |    |     |   |   |        |    |    |    |    |     |
| Option D: | $\frac{15}{17}$   |    |    |    |     |   |   |        |    |    |    |    |     |
|           |   |    |    |    |     |   |   |        |    |    |    |    |     |
| Q15.      | The number of pendent vertices in a binary tree with 15 vertices is   |    |    |    |     |   |   |        |    |    |    |    |     |

|           |  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
|-----------|--|----|----|----|----|----|----|----|----|----|---|----|----|----|----|----|----|----|----|
| Option A: | 6  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option B: | 7  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option C: | 8  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option D: | 9  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Q16.      | Given that $A = \{2, 3, 6, 12, 24, 36, 72\}$ is a poset under the relation divisibility. Find $2 \wedge 3$ .   |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option A: | 6  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option B: | 12   |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option C: | 2  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option D: | Does not exist   |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Q17.      | Let $R$ be the group of all non-zero real numbers under the operation $a * b = 2ab$ . The Identity element of the group $(R, *)$ is _____  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option A: | $\frac{1}{2}$  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option B: | 3  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option C: | 2  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option D: | $\frac{1}{3}$  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Q18.      | The number of vertices in 5 – Regular Graph with 20 edges is   |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option A: | 6  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option B: | 8  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option C: | 10   |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option D: | 12   |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Q19.      | The remainder when 5 divides $(56)^{111}$ is _____   |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option A: | 2  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option B: | 1  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option C: | 0  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option D: | 4  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Q20.      | The correlation coefficient $r$ for the following data is  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
|           | <table border="1"> <tbody> <tr> <td>X</td><td>65</td><td>66</td><td>67</td><td>67</td><td>68</td><td>69</td><td>70</td><td>72</td></tr> <tr> <td>Y</td><td>67</td><td>68</td><td>65</td><td>68</td><td>72</td><td>72</td><td>69</td><td>71</td></tr> </tbody> </table> | X  | 65 | 66 | 67 | 67 | 68 | 69 | 70 | 72 | Y | 67 | 68 | 65 | 68 | 72 | 72 | 69 | 71 |
| X         | 65   | 66 | 67 | 67 | 68 | 69 | 70 | 72 |    |    |   |    |    |    |    |    |    |    |    |
| Y         | 67   | 68 | 65 | 68 | 72 | 72 | 69 | 71 |    |    |   |    |    |    |    |    |    |    |    |
| Option A: | 0.572  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option B: | -0.264   |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option C: | 0.974  |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |
| Option D: | 0.6030   |    |    |    |    |    |    |    |    |    |   |    |    |    |    |    |    |    |    |

|           |   |
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| Q21.      | Given that $Z_5 = \{0, 1, 2, 3, 4\}$ is a group under addition modulo 5.<br>Find the inverse of the element 3.            |
| Option A: | 0   |
| Option B: | 1   |
| Option C: | 2   |
| Option D: | 4   |
| Q22.      | If a random variable X follows Poisson distribution such that<br>$P(X = 1) = 2P(X = 2)$ then find the value of $P(X = 4)$ |
| Option A: | 0.07754   |
| Option B: | 0.01532   |
| Option C: | 0.08945   |
| Option D: | 0.06879   |
| Q23.      | The equations of the two regression lines are<br>$3x + 2y = 26$ & $6x + y = 31$ . Find the correlation coefficient r.     |
| Option A: | 0.65  |
| Option B: | 0.79  |
| Option C: | -0.5  |
| Option D: | 0.87  |
| Q24.      | Given that $L = \{1, 2, 3, 4, 12\}$ is a Lattice under the relation divisibility.<br>Find complement of the element 4.    |
| Option A: | 1   |
| Option B: | 2   |
| Option C: | 12  |
| Option D: | 3   |
| Q25.      | Find $x$ if $5^{31} \equiv x \pmod{31}$   |
| Option A: | 31  |
| Option B: | 25  |
| Option C: | 5   |
| Option D: | 15  |